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Introduction

A compiler was originally a program that “compiled” subroutines [a link-loader]. When in 1954 the combination “algebraic compiler” came into use, or rather into misuse, the meaning of the term had already shifted into the present one.

Bauer and Eickel [1975]

This book describes techniques, data structures, and algorithms for translating programming languages into executable code. A modern compiler is often organized into many phases, each operating on a different abstract “language.” The chapters of this book follow the organization of a compiler, each covering a successive phase.

To illustrate the issues in compiling real programming languages, we show how to compile MiniJava, a simple but nontrivial subset of Java. Programming exercises in each chapter call for the implementation of the corresponding phase; a student who implements all the phases described in Part I of the book will have a working compiler. MiniJava is easily extended to support class extension or higher-order functions, and exercises in Part II show how to do this. Other chapters in Part II cover advanced techniques in program optimization. Appendix A describes the MiniJava language.

The interfaces between modules of the compiler are almost as important as the algorithms inside the modules. To describe the interfaces concretely, it is useful to write them down in a real programming language. This book uses Java—a simple object-oriented language. Java is safe, in that programs cannot circumvent the type system to violate abstractions; and it has garbage collection, which greatly simplifies the management of dynamic storage al-
location. Both of these properties are useful in writing compilers (and almost any kind of software).

This is not a textbook on Java programming. Students using this book who do not know Java already should pick it up as they go along, using a Java programming book as a reference. Java is a small enough language, with simple enough concepts, that this should not be difficult for students with good programming skills in other languages.

1.1 MODULES AND INTERFACES

Any large software system is much easier to understand and implement if the designer takes care with the fundamental abstractions and interfaces. Figure 1.1 shows the phases in a typical compiler. Each phase is implemented as one or more software modules.

Breaking the compiler into this many pieces allows for reuse of the components. For example, to change the target machine for which the compiler pro-
duces machine language, it suffices to replace just the Frame Layout and Instruction Selection modules. To change the source language being compiled, only the modules up through Translate need to be changed. The compiler can be attached to a language-oriented syntax editor at the Abstract Syntax interface.

The learning experience of coming to the right abstraction by several iterations of think–implement–redesign is one that should not be missed. However, the student trying to finish a compiler project in one semester does not have this luxury. Therefore, we present in this book the outline of a project where the abstractions and interfaces are carefully thought out, and are as elegant and general as we are able to make them.

Some of the interfaces, such as Abstract Syntax, IR Trees, and Assem, take the form of data structures: For example, the Parsing Actions phase builds an Abstract Syntax data structure and passes it to the Semantic Analysis phase. Other interfaces are abstract data types; the Translate interface is a set of functions that the Semantic Analysis phase can call, and the Tokens interface takes the form of a function that the Parser calls to get the next token of the input program.

**DESCRIPTION OF THE PHASES**

Each chapter of Part I of this book describes one compiler phase, as shown in Table 1.2

This modularization is typical of many real compilers. But some compilers combine Parse, Semantic Analysis, Translate, and Canonicalize into one phase; others put Instruction Selection much later than we have done, and combine it with Code Emission. Simple compilers omit the Control Flow Analysis, Data Flow Analysis, and Register Allocation phases.

We have designed the compiler in this book to be as simple as possible, but no simpler. In particular, in those places where corners are cut to simplify the implementation, the structure of the compiler allows for the addition of more optimization or fancier semantics without violence to the existing interfaces.

**TOOLS AND SOFTWARE**

Two of the most useful abstractions used in modern compilers are context-free grammars, for parsing, and regular expressions, for lexical analysis. To make the best use of these abstractions it is helpful to have special tools,
### TABLE 1.2. Description of compiler phases.

<table>
<thead>
<tr>
<th>Chapter</th>
<th>Phase</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>2</td>
<td>Lex</td>
<td>Break the source file into individual words, or <em>tokens</em>.</td>
</tr>
<tr>
<td>3</td>
<td>Parse</td>
<td>Analyze the phrase structure of the program.</td>
</tr>
<tr>
<td>4</td>
<td>Semantic</td>
<td>Build a piece of <em>abstract syntax tree</em> corresponding to each phrase.</td>
</tr>
<tr>
<td></td>
<td>Actions</td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>Semantic</td>
<td>Determine what each phrase means, relate uses of variables to their definitions, check types of expressions, request translation of each phrase.</td>
</tr>
<tr>
<td></td>
<td>Analysis</td>
<td></td>
</tr>
<tr>
<td>6</td>
<td>Frame</td>
<td>Place variables, function-parameters, etc. into activation records (stack frames) in a machine-dependent way.</td>
</tr>
<tr>
<td></td>
<td>Layout</td>
<td></td>
</tr>
<tr>
<td>7</td>
<td>Translate</td>
<td>Produce <em>intermediate representation trees</em> (IR trees), a notation that is not tied to any particular source language or target-machine architecture.</td>
</tr>
<tr>
<td>8</td>
<td>Canonicalize</td>
<td>Hoist side effects out of expressions, and clean up conditional branches, for the convenience of the next phases.</td>
</tr>
<tr>
<td>9</td>
<td>Instruction</td>
<td>Group the IR-tree nodes into clumps that correspond to the actions of target-machine instructions.</td>
</tr>
<tr>
<td></td>
<td>Selection</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>Control</td>
<td>Analyze the sequence of instructions into a <em>control flow graph</em> that shows all the possible flows of control the program might follow when it executes.</td>
</tr>
<tr>
<td></td>
<td>Flow</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Analysis</td>
<td></td>
</tr>
<tr>
<td>10</td>
<td>Dataflow</td>
<td>Gather information about the flow of information through variables of the program; for example, <em>liveness analysis</em> calculates the places where each program variable holds a still-needed value (is live).</td>
</tr>
<tr>
<td></td>
<td>Analysis</td>
<td></td>
</tr>
<tr>
<td>11</td>
<td>Register</td>
<td>Choose a register to hold each of the variables and temporary values used by the program; variables not live at the same time can share the same register.</td>
</tr>
<tr>
<td></td>
<td>Allocation</td>
<td></td>
</tr>
<tr>
<td>12</td>
<td>Code</td>
<td>Replace the temporary names in each machine instruction with machine registers.</td>
</tr>
<tr>
<td></td>
<td>Emission</td>
<td></td>
</tr>
</tbody>
</table>

such as *Yacc* (which converts a grammar into a parsing program) and *Lex* (which converts a declarative specification into a lexical-analysis program). Fortunately, such tools are available for Java, and the project described in this book makes use of them.

The programming projects in this book can be compiled using any Java
1.3. DATA STRUCTURES FOR TREE LANGUAGES

Many of the important data structures used in a compiler are intermediate representations of the program being compiled. Often these representations take the form of trees, with several node types, each of which has different attributes. Such trees can occur at many of the phase-interfaces shown in Figure 1.1.

Tree representations can be described with grammars, just like programming languages. To introduce the concepts, we will show a simple programming language with statements and expressions, but no loops or if-statements (this is called a language of straight-line programs).

The syntax for this language is given in Grammar 1.3.

The informal semantics of the language is as follows. Each \( Stm \) is a statement, each \( Exp \) is an expression. \( s_1; s_2 \) executes statement \( s_1 \), then statement \( s_2 \). \( i := e \) evaluates the expression \( e \), then “stores” the result in variable \( i \).

**Grammar 1.3.** A straight-line programming language.

```
Stm → Stm ; Stm (CompoundStm)
Stm → id := Exp (AssignStm)
Stm → print ( ExpList ) (PrintStm)
Exp → id (IdExp)
Exp → num (NumExp)
Exp → Exp Binop Exp (OpExp)
Exp → ( Stm , Exp ) (EseqExp)
ExpList → Exp , ExpList (PairExpList)
ExpList → Exp (LastExpList)
Binop → + (Plus)
Binop → − (Minus)
Binop → × (Times)
Binop → / (Div)
```
print($e_1, e_2, \ldots, e_n$) displays the values of all the expressions, evaluated left to right, separated by spaces, terminated by a newline.

An **identifier expression**, such as $i$, yields the current contents of the variable $i$. A **number** evaluates to the named integer. An **operator expression** $e_1 \text{ op } e_2$ evaluates $e_1$, then $e_2$, then applies the given binary operator. And an **expression sequence** ($s, e$) behaves like the C-language “comma” operator, evaluating the statement $s$ for side effects before evaluating (and returning the result of) the expression $e$.

For example, executing this program

```plaintext
a := 5+3; b := (print(a, a-1), 10*a); print(b)
```

prints

```
8 7
80
```

How should this program be represented inside a compiler? One representation is **source code**, the characters that the programmer writes. But that is not so easy to manipulate. More convenient is a tree data structure, with one node for each statement (Stm) and expression (Exp). Figure 1.4 shows a tree representation of the program; the nodes are labeled by the production labels of Grammar 1.3, and each node has as many children as the corresponding grammar production has right-hand-side symbols.

We can translate the grammar directly into data structure definitions, as shown in Program 1.5. Each grammar symbol corresponds to an **abstract class** in the data structures:

<table>
<thead>
<tr>
<th>Grammar</th>
<th>class</th>
</tr>
</thead>
<tbody>
<tr>
<td>Stm</td>
<td>Stm</td>
</tr>
<tr>
<td>Exp</td>
<td>Exp</td>
</tr>
<tr>
<td>ExpList</td>
<td>ExpList</td>
</tr>
<tr>
<td>id</td>
<td>String</td>
</tr>
<tr>
<td>num</td>
<td>int</td>
</tr>
</tbody>
</table>

For each grammar rule, there is one **constructor** that belongs to the class for its left-hand-side symbol. We simply **extend** the abstract class with a “concrete” class for each grammar rule. The constructor (class) names are indicated on the right-hand side of Grammar 1.3.

Each grammar rule has right-hand-side components that must be represented in the data structures. The CompoundStm has two Stm’s on the right-hand side; the AssignStm has an identifier and an expression; and so on.
These become fields of the subclasses in the Java data structure. Thus, CompoundStm has two fields (also called instance variables) called stm1 and stm2; AssignStm has fields id and exp.

For Binop we do something simpler. Although we could make a Binop class – with subclasses for Plus, Minus, Times, Div – this is overkill because none of the subclasses would need any fields. Instead we make an “enumeration” type (in Java, actually an integer) of constants (final int variables) local to the OpExp class.

**Programming style.** We will follow several conventions for representing tree data structures in Java:

1. Trees are described by a grammar.
2. A tree is described by one or more abstract classes, each corresponding to a symbol in the grammar.
3. Each abstract class is extended by one or more subclasses, one for each grammar rule.
public abstract class Stm {}

public class CompoundStm extends Stm {
    public Stm stm1, stm2;
    public CompoundStm(Stm s1, Stm s2) {stm1=s1; stm2=s2;}
}

public class AssignStm extends Stm {
    public String id; public Exp exp;
    public AssignStm(String i, Exp e) {id=i; exp=e;}
}

public class PrintStm extends Stm {
    public ExpList exps;
    public PrintStm(ExpList e) {exps=e;}
}

public abstract class Exp {}

public class IdExp extends Exp {
    public String id;
    public IdExp(String i) {id=i;}
}

public class NumExp extends Exp {
    public int num;
    public NumExp(int n) {num=n;}
}

public class OpExp extends Exp {
    public Exp left, right; public int oper;
    final public static int Plus=1, Minus=2, Times=3, Div=4;
    public OpExp(Exp l, int o, Exp r) {left=l; oper=o; right=r;}
}

public class EseqExp extends Exp {
    public Stm stm; public Exp exp;
    public EseqExp(Stm s, Exp e) {stm=s; exp=e;}
}

public abstract class ExpList {}

public class PairExpList extends ExpList {
    public Exp head; public ExpList tail;
    public PairExpList(Exp h, ExpList t) {head=h; tail=t;}
}

public class LastExpList extends ExpList {
    public Exp head;
    public LastExpList(Exp h) {head=h;}
}

PROGRAM 1.5. Representation of straight-line programs.
4. For each nontrivial symbol in the right-hand side of a rule, there will be one field in the corresponding class. (A trivial symbol is a punctuation symbol such as the semicolon in CompoundStm.)

5. Every class will have a constructor function that initializes all the fields.

6. Data structures are initialized when they are created (by the constructor functions), and are never modified after that (until they are eventually discarded).

**Modularity principles for Java programs.** A compiler can be a big program; careful attention to modules and interfaces prevents chaos. We will use these principles in writing a compiler in Java:

1. Each phase or module of the compiler belongs in its own package.

2. “Import on demand” declarations will not be used. If a Java file begins with
   ```java
   import A.F.*; import A.G.*; import B.*; import C.*;
   ```
   then the human reader *will have to look outside this file* to tell which package defines the X that is used in the expression `X.put()`.

3. “Single-type import” declarations are a better solution. If the module begins
   ```java
   import A.F.W; import A.G.X; import B.Y; import C.Z;
   ```
   then you can tell *without looking outside this file* that X comes from A.G.

4. Java is naturally a multithreaded system. We would like to support multiple simultaneous compiler threads and compile two different programs simultaneously, one in each compiler thread. Therefore, static variables must be avoided unless they are `final` (constant). We never want two compiler threads to be updating the same (static) instance of a variable.

**PROGRAM STRAIGHT-LINE PROGRAM INTERPRETER**

Implement a simple program analyzer and interpreter for the straight-line programming language. This exercise serves as an introduction to *environments* (symbol tables mapping variable names to information about the variables); to *abstract syntax* (data structures representing the phrase structure of programs); to *recursion over tree data structures*, useful in many parts of a compiler; and to a *functional style* of programming without assignment statements.

It also serves as a “warm-up” exercise in Java programming. Programmers experienced in other languages but new to Java should be able to do this exercise, but will need supplementary material (such as textbooks) on Java.

Programs to be interpreted are already parsed into abstract syntax, as described by the data types in Program 1.5.

However, we do not wish to worry about parsing the language, so we write this program by applying data constructors:
CHAPTER ONE. INTRODUCTION

```java
Stm prog =
new CompoundStm(new AssignStm("a",
    new OpExp(new NumExp(5),
        OpExp.Plus, new NumExp(3))),
new CompoundStm(new AssignStm("b",
    new EseqExp(new PrintStm(new PairExpList(new IdExp("a"),
            new LastExpList(new OpExp(new IdExp("a"),
                        OpExp.Minus,new NumExp(1))))),
new OpExp(new NumExp(10), OpExp.Times,
            new IdExp("a")))),
new PrintStm(new LastExpList(new IdExp("b")))));
```

Files with the data type declarations for the trees, and this sample program, are available in the directory `$MINIJAVA/chap1`.

Writing interpreters without side effects (that is, assignment statements that update variables and data structures) is a good introduction to denotational semantics and attribute grammars, which are methods for describing what programming languages do. It’s often a useful technique in writing compilers, too; compilers are also in the business of saying what programming languages do.

Therefore, in implementing these programs, never assign a new value to any variable or object field except when it is initialized. For local variables, use the initializing form of declaration (for example, `int i=j+3;`) and for each class, make a constructor function (like the `CompoundStm` constructor in Program 1.5).

1. Write a Java function `int maxargs(Stm s)` that tells the maximum number of arguments of any print statement within any subexpression of a given statement. For example, `maxargs(prog)` is 2.

2. Write a Java function `void interp(Stm s)` that “interprets” a program in this language. To write in a “functional programming” style – in which you never use an assignment statement – initialize each local variable as you declare it.

Your functions that examine each `Exp` will have to use `instanceof` to determine which subclass the expression belongs to and then cast to the proper subclass. Or you can add methods to the `Exp` and `Stm` classes to avoid the use of `instanceof`.

For part 1, remember that print statements can contain expressions that contain other print statements.
For part 2, make two mutually recursive functions interpStmt and interpExp. Represent a “table,” mapping identifiers to the integer values assigned to them, as a list of id × int pairs.

```java
class Table {
    String id; int value; Table tail;
    Table(String i, int v, Table t) {id=i; value=v; tail=t;}
}
```

Then interpStmt is declared as

```java
Table interpStmt(Stm s, Table t)
```

taking a table \( t_1 \) as argument and producing the new table \( t_2 \) that’s just like \( t_1 \) except that some identifiers map to different integers as a result of the statement.

For example, the table \( t_1 \) that maps \( a \) to 3 and maps \( c \) to 4, which we write \( \{ a \mapsto 3, c \mapsto 4 \} \) in mathematical notation, could be represented as the linked list \( a 3 \rightarrow c 4 \).

Now, let the table \( t_2 \) be just like \( t_1 \), except that it maps \( c \) to 7 instead of 4. Mathematically, we could write,

\[
t_2 = \text{update}(t_1, c, 7),
\]

where the update function returns a new table \( \{ a \mapsto 3, c \mapsto 7 \} \).

On the computer, we could implement \( t_2 \) by putting a new cell at the head of the linked list: \( \overbrace{c 7} \rightarrow \overbrace{a 3} \rightarrow \overbrace{c 4} \), as long as we assume that the *first* occurrence of \( c \) in the list takes precedence over any later occurrence.

Therefore, the update function is easy to implement; and the corresponding lookup function

```java
int lookup(Table t, String key)
```

just searches down the linked list. Of course, in an object-oriented style, \( \text{int lookup(String key)} \) should be a method of the Table class.

Interpreting expressions is more complicated than interpreting statements, because expressions return integer values *and* have side effects. We wish to simulate the straight-line programming language’s assignment statements without doing any side effects in the interpreter itself. (The print statements will be accomplished by interpreter side effects, however.) The solution is to declare interpExp as
class IntAndTable {int i; Table t;
    IntAndTable(int ii, Table tt) {i=ii; t=tt;}
}

IntAndTable interpExp(Exp e, Table t) ...

The result of interpreting an expression $e_1$ with table $t_1$ is an integer value $i$ and a new table $t_2$. When interpreting an expression with two subexpressions (such as an OpExp), the table $t_2$ resulting from the first subexpression can be used in processing the second subexpression.

**EXERCISES**

1.1 This simple program implements persistent functional binary search trees, so that if $\text{tree2}=\text{insert}(x,\text{tree1})$, then $\text{tree1}$ is still available for lookups even while $\text{tree2}$ can be used.

```java
class Tree {Tree left; String key; Tree right;
    Tree(Tree l, String k, Tree r) {left=l; key=k; right=r;}

    Tree insert(String key, Tree t) {
        if (t==null) return new Tree(null, key, null)
        else if (key.compareTo(t.key) < 0)
            return new Tree(insert(key,t.left),t.key,t.right);
        else if (key.compareTo(t.key) > 0)
            return new Tree(t.left,t.key,insert(key,t.right));
        else return new Tree(t.left,key,t.right);
    }
}
```

a. Implement a member function that returns true if the item is found, else false.

b. Extend the program to include not just membership, but the mapping of keys to bindings:

```java
    Tree insert(String key, Object binding, Tree t);
    Object lookup(String key, Tree t);
```

c. These trees are not balanced; demonstrate the behavior on the following two sequences of insertions:

- (a) t s p i p f b s t
- (b) a b c d e f g h i

*d. Research balanced search trees in Sedgewick [1997] and recommend a balanced-tree data structure for functional symbol tables. **Hint:** To preserve a functional style, the algorithm should be one that rebalances
on insertion but not on lookup, so a data structure such as splay trees is not appropriate.

e. Rewrite in an object-oriented (but still “functional”) style, so that insertion is now `t.insert(key)` instead of `insert(key,t)`. **Hint:** You’ll need an `EmptyTree` subclass.